

A statistical approach to the prediction of pK_a values in proteins

Yun He,^{1,3} Jialin Xu,² and Xian-Ming Pan^{1,2*}

¹National Laboratory of Biomacromolecules, Institute of Biophysics, Chinese Academy of Sciences, Beijing 100101, China

²Department of Biological Sciences and Biotechnology, Tsinghua University, Beijing 100084, China

³Graduate University of Chinese Academy of Sciences, Beijing 100049, China

ABSTRACT

We propose a simple model for the calculation of pK_a values of ionizable residues in proteins. It is based on the premise that the pK_a shift of ionizable residues is linearly correlated to the interaction between a particular residue and the local environment created by the surrounding residues. Despite its simplicity, the model displays good prediction performance. Under the sixfold cross test prediction over a data set of 405 experimental pK_a values in 73 protein chains with known structures, the root-mean-square deviation (RMSD) between the experimental and calculated pK_a was found to be 0.77. The accuracy of this model increases with increasing size of the data set: the RMSD is 0.609 for glutamate (the largest data set with 141 sites) and ~ 1 pH unit for lysine, with a data set containing 45 sites.

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Key words: protein ionizable residues pK_a prediction; residue interaction; protonation; deprotonation; electrostatic interaction.

INTRODUCTION

Ionizable residues play key roles in biological processes involving proteins, including ligand binding, protein–protein interaction, and protein folding and unfolding. For example, the structure and function of many proteins are dependent on the protonation equilibrium of ionizable residues. Most enzymes perform catalysis with the assistance of ionizable residues that either act directly as acids, bases, and ligands, or less directly through effects on the electrostatic potential at or near the active site.¹ The distribution of surface-charged residues is critical for protein–protein association.² Many proteins denature when the pH is changed to very low or very high values. The primary reason for denaturation at extreme pH is that proteins usually have buried residues with highly perturbed pK_a values.³

Knowledge of the pK_a values of ionizable residues enables the prediction of the protonation state at a given pH, which is often essential in the prediction of protein properties.⁴ However, it is also well recognized that structural and environmental features of the protein can influence the protonation state. For example, pK_a values of solvent-exposed carboxylic residues show little variation and have relatively narrow distributions, while pK_a values for buried residues can range from 2 to 6.7.⁵ Considering these factors, it is not surprising that many experimentally determined pK_a values are very different from those derived from model compounds in solution. These effects are referred to as perturbations of the pK_a values, and present a significant barrier to accurate prediction of protein properties.

The pK_a values of ionizable residues can be determined experimentally by nuclear magnetic resonance (NMR), but the applicability of this technique is limited by protein size and solubility.^{6–10} On the other hand, there has been a great deal of activity in the fields of computational biology and computational chemistry aimed at developing theoretical methods for calculation of pK_a values in proteins. Most of these theoretical methods employ various treatments to give quantitative descriptions of electrostatic effects, such as free-energy perturbation (FEP) approaches,¹¹ protein dipole Langevin dipole (PDL) and PDL/S-LRA approaches,^{12,13} Tanford Kirkwood (TK)¹⁴ and modified TK models,¹⁵ as well as popularly applied Poisson Boltzmann (PB) approaches,¹⁶ which have been described a lot in reviews^{4,12,16–19} and other articles.^{11,13–15,20–33} These methods have given encouraging results that could provide useful insights into the structure–function correlator for proteins. However, the

The web server that implements our statistical model for the prediction of pK_a values in proteins is freely accessible at <http://spg.biosci.tsinghua.edu.cn/~jarod/pkacal/submitjob.cgi>.

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*Correspondence to: Xian-Ming Pan, Department of Biological Sciences and Biotechnology, Tsinghua University, Beijing 100084, China. E-mail: pan-xm@mail.tsinghua.edu.cn

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results of macroscopic models depend critically on the choice of protein dielectric constant whose concept is problematic, while the microscopic models are entirely practical but require professional treatment, which has been provided by some research groups.^{4,19}

Nowadays, with an increasing number of experimentally available pK_a values for proteins with known structure, prediction of pK_a values by means of the empirical parameterization of the protein pK_a database becomes feasible.^{5,34–36} These empirical methods yield a root-mean-square deviation (RMSD) of ~ 1 pH unit. This performance is comparable to theoretical models, but is achieved with greater speed and ease of use. Wisz and Hellinga³⁴ modeled solvent and interior effects using multiple dielectric constants obtained by fitting to experimental pK_a values. Godoy-Ruiz *et al.*³⁵ employed a genetic algorithm to empirically parameterize pK_a values for carboxylic acids in proteins. Li *et al.*³⁶ presented an empirical method in a study of the molecular determinants of pK_a values of Asp and Glu in the protein turkey ovomucoid third domain (OMTKY3). They took into account three types of pK_a perturbation: hydrogen bonding, desolvation, and charge–charge interactions, in which hydrogen bonds were identified as the prime pK_a determinant. However, the pK_a values were determined by changing the pH within a range centered on the pK_a value of the residue of interest, while hydrogen bonds were identified based on the X-ray or NMR structure determined at a given pH.

Here, we present a very simple model derived from statistical theory to predict protein pK_a values. It is based on the premise that the pK_a shift of ionizable residues in proteins is linearly correlated to the interaction between a given residue and its surrounding residues. Despite its relative simplicity, the model is quite able to reproduce experimental results. Its principal shortcoming is the dependence on the size of the data set. The current data set is too small to derive prediction coefficients for internal residues that tend to have highly shifted pK_a values and are often catalytically important, and the coefficients derived from surface residues are not suitable for extending the application in internal residues.

MATERIALS AND METHODS

The pK_a database

A large collection of high quality experimental pK_a values is essential to the development and assessment of this new method. Researchers at the Edward Jenner Institute have been maintaining a protein pK_a database named PPD (URL: <http://www.jenner.ac.uk/PPD/>), which is the largest and the most comprehensive collection of experimentally identified pK_a values. Unfortunately, the PPD web site does not provide a downloadable database in flat text or other human-readable format. For conven-

ience, we recompiled a subset of experimental pK_a values derived from PPD.

By extracting pK_a values from the PPD web site and manually validating the data using experimental 3D structures from PDB (URL: <http://www.rcsb.org>), we obtained a subset of experimentally measured pK_a values containing 1122 pK_a values belonging to 667 unique dissociable sites (as of July, 2006). To minimize the side-effect of potentially contradictory experimental data, we filtered our data set based on the following rules: (a) pK_a values identified by NMR methods were accepted; (b) pK_a values for a single site differing by more than 1.0 when determined by separate experiments or a standard deviation (SD) greater than 0.5 were filtered out; (c) pK_a values with a sequential number recorded in PPD inconsistent with that of PDB due to, for example, mutants or lack of crystal data were also excluded. After filtration, we obtained a collection of 475 unique sites located in 73 protein chains in which each site has only one experimental pK_a value assigned (if the site had multiple pK_a values, the average value was assigned instead), listed in Table I. In the data set, the pK_a values of 46 sites are unusual because of physical or chemical factors, such as salt bridges or disulfide bridges (Table II). To obtain reasonable parameters, these data were excluded from the fitting procedure and were predicted using the parameters obtained from the remaining sites. Figure 1 depicts the histogram of pK_a values for the residues Asp, Glu, His, and Lys.

Model for pK_a calculation

The difference in pK_a between an amino acid residue in a protein and that of the amino acid in solution can be expressed as:

$$pK = pK^{\text{mod}} + \frac{1}{2.3RT} \Delta\Delta G \quad (1)$$

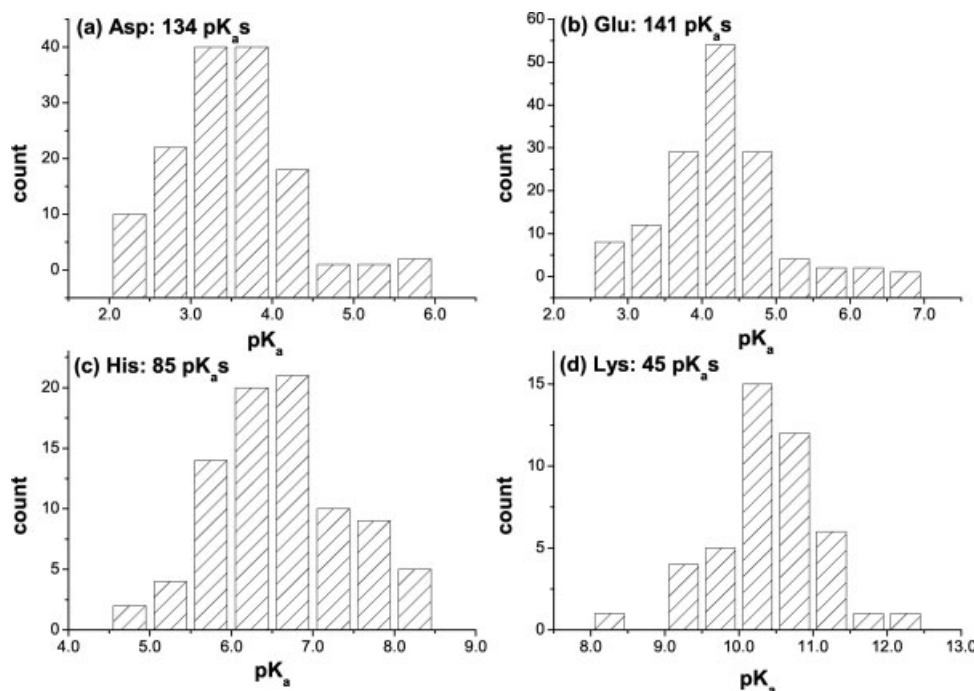
In Eq. (1), R is the gas constant and T is the temperature (usually 298 K). The term $\Delta\Delta G$ is the difference in free energies of deprotonation in the model compound and in the protein. Because of the complex nature of $\Delta\Delta G$, the pK_a shift can be viewed as consisting of two parts: (1) transfer from the model compound to the pro-

Table I
Statistics for the 475 pK_a Values

Residue	Number	Average	Min	Max	SD
Asp	150	3.47	1.40	9.90	1.22
Glu	146	4.16	2.10	7.60	0.81
His	96	6.30	2.30	9.20	1.37
Cys	8	4.67	2.23	8.80	2.91
Tyr	28	9.90	2.09	12.50	2.62
Lys	47	10.04	2.21	12.05	1.73

Table IIList of pK_a Values with Large Deviation from the pK_a Values of Model Compounds

PDB	Residue		pK _a	Note	Reference
1A2P	A:73	E	2.10	D93 forms a salt link with R69 and titrates at much lower pH values.	6
	A:93	D	2.00		
	A:101	D	2.00		
1A91	61	D	7.0	D61 is thought to protonate and deprotonate during each proton translocation cycle. This pK _a was significantly higher.	37
1CDC	A:41	E	6.7	E41 is on the binding surface of rat CD2 with an unusually elevated pK _a , and the electrostatic interaction with the E29 side chain is a significant contributing influence.	38
1D3K	A:45	Y	7.09	The low pK _a values of tyrosines are due to the electrostatic interactions with the neighboring groups. The low pK _a of Y188 is due to the iron-binding ligand interactions with K206 in open-form and with K296 in the closed-form of the protein.	39
	A:85	Y	8.01		
	A:96	Y	7.06		
	A:188	Y	6.86		
1HIC	39	C	3.76	The carboxyl of D25 (chain A) is protonated while that of D125 (chain B) is not protonated. The side chain of D25 is protonated in order to donate a hydrogen bond to carbonyl oxygen of KNI-272.	40
1HPX	A:25	D	6.20		
1L63	31	H	9.10	A salt bridge formed between the side chains of D70 and H31 contributes the perturbation of pK _a values in the native state.	42
	70	D	1.40		
1LYS	A:66	D	2.00	The pK _a of D66 is inaccurate because of an insufficient number of chemical shift values obtained at low pH.	43
1LZ3	66	D	2.00		
1M8B	A:56	C	2.27	Salt bridges are established between E (B13) and H (B10).	44
1M8C	A:56	C	2.27		
1MHI	A:19	Y	2.87		
	B:5	H	3.75		
	B:10	H	2.66		
	B:13	E	2.45		
1MUT	B:16	Y	2.09	E53 is functioning as a base catalyst in the active quaternary complex.	46
	53	E	7.60		
10MU	31	Y	12.50	C56 forms disulfide bridge with C24. The very high pK _a of Y31 may be attributed to a short hydrogen bond with D27 and its low solvent accessible surface area.	47
	56	C	2.50		
1PNT	72	H	9.20	The high pK _a is hypothesized to be caused by electrostatic interactions with nearby negatively charged groups (E23 and D42).	48
1QH7	A:60	H	4.01	The low pK _a of H60 provides a hint of an unusual microenvironment, despite the electrostatic influence of E167 which would be expected to elevate the pK _a . The low pK _a of H162 reflects the buried hydrophobic environment of the imidazole ring within the enzyme.	49
	A:162	H	2.70		
1RGG	A:79	D	7.37	D79, which is buried but does not form hydrogen bonds, has the most elevated pK _a .	10
1RNZ	14	D	1.90	The four histidine residues are neutrally charged and do not titrate.	n/a
1SBT	17	H	3.00		
	39	H	3.00		
	67	H	3.00		
	226	H	3.00		
1SPU	A:383	D	9.70	The high pK _a is due to the fact that the deprotonation disrupts the hydrogen-bonding interaction with the pyridine nitrogen of the 2HP moiety.	51
1SSO	18	K	3.00	K18 is involved in both a salt bridge and an H-bond.	52
1TRS	26	D	8.10	In both the reduced and the oxidized states of human thioredoxin, the stabilization of the protonated side chain of D26 is achieved via a hydrogen-bonding network involving the hydroxyl group of the neighboring S28.	53
1TRW	26	D	9.90		
1XNB	83	D	2.00	D83 is completely buried, forming a strong salt bridge with R136. D101 is located on the surface of the protein, stabilized in the deprotonated form by an extensive network of hydrogen bonds. H149 is completely buried within the hydrophobic core and is involved in an extensive network of hydrogen bonding interactions. E172 plays a role of the acid/base catalyst.	54,55
	101	D	2.00		
	149	H	2.30		
	172	E	6.70		
20VO	29	K	2.21	The low pK _a for the α-carboxyl group of C56 is attributed to acidification by the disulfide group.	56
	56	C	2.23		
2RN2	102	D	2.00		57
	148	D	2.00		

**Figure 1**

Distributions of pK_a values in proteins: (a) 134 Asp, (b) 141 Glu, (c) 85 His and (d) 45 Lys. Each column entry represents the number of pK_a values, in 0.5 pH unit increments.

tein neglecting interactions with other sites, giving the intrinsic pK_a (pK_a^{intr}); (2) site–site interactions resulting in an additional shift in the pK_a .¹⁷ Therefore, the term $\Delta\Delta G$ can be separated into a site–site interaction term (ΔG_{ss}) and an intrinsic term (ΔG_{intr}), and Eq. (1) can be rewritten as:

$$\begin{aligned} pK &= pK^{\text{mod}} + \frac{1}{2.3RT} \Delta\Delta G \\ &= pK^{\text{mod}} + \frac{1}{2.3RT} (\Delta G_{\text{ss}} + \Delta G_{\text{intr}}) = pK^{\text{intr}} + \frac{1}{2.3RT} \Delta G_{\text{ss}} \end{aligned} \quad (2)$$

Here, we adopt a simplified model for calculating pK_a . The main issues are as follows.

To avoid estimating pK_a^{intr} in Eq. (2), we instead used pK_a^0 (the average pK_a value found in the data set of the corresponding residues) as a reference state. Since the experimental pK_a values display a normal distribution, the value of pK_a^0 differs from the intrinsic pK_a^{intr} only by a constant.

The pK_a value of a given residue i can then be described as:

$$pK_i = pK_i^0 + \frac{1}{2.3RT} \Delta G_i \quad (3)$$

The model described here assumes that the interaction between the residue of interest and the surrounding resi-

dues is the dominant influence on pK_a , and that interactions with more distant residues can be neglected because of shielding by the neighboring residues. To simplify the calculation, we defined a sphere with a fixed radius centered at the $C\alpha$ atom of the residue of interest and calculated the pK_a shift using only residues whose $C\alpha$ atom was located within the sphere.

NMR experiments to determine protein pK_a values indicate that with a few exceptions, the pH dependency of chemical shifts of ionizable residues could be fitted by the Henderson-Hasselbach equation.^{6–10} This indicates that the free energy change of the proton binding reaction is unchanged by variations in pH, although the residues undergo changes in charge state and the protein constantly experiences conformational fluctuations. We therefore assume that the pK_a shift is a function of the amino acids in the sphere:

$$pK_i = pK_i^0 + f(n_1, n_2, \dots, n_{20}) \quad (4)$$

Here n_j ($j = 1–20$) is the number of j th amino acid located in the sphere, and the function $f(n_1, n_2, \dots, n_{20})$ is unknown.

The function $f(n_1, n_2, \dots, n_{20})$ is obtained by a statistical approach. According to statistical principles, if n_1, n_2, \dots, n_{20} are independent random variables, their linear combination is a normal distribution. For simplification,

we assume that the pK_a shift induced by residue–residue interaction is a linear function of the amino acids around the ionizable residue:

$$pK_i = pK_i^0 + \sum_{j=1}^{20} c_{ij}n_{ij} \quad (5)$$

Here i ($i = 1-7$) for the ionizable residues Asp, Glu, His, Cys, Tyr, Arg and Lys, and j ($j = 1-20$) for 20 amino acids with N-termini represented as an analog of Lys and C-termini as an analog of Asp. c_{ij} denotes the coefficients for the residue–residue interaction term for residue i with another residue j , and n_{ij} denotes the number of residue j around the residue i .

Fitting procedure with multiple linear regression method

The coefficients c_{ij} were determined from the data in the training set using the multiple linear regression method to minimize the sum of the square of deviations between the left and the right side of the equation.^{58,59} In addition to a self-consistency validation, a sixfold cross validation was performed. The 73 protein chains were randomly placed into six groups and each group in turn was predicted using the coefficients obtained using the remaining groups as a training set. Since the data size for Cys and Tyr were too small to determine the coefficients c_{ij} , predictions of Cys and Tyr were performed using the coefficients of residue His.

RESULTS

The model used here assumes that the interaction between the residue of interest and its close neighbors is the dominant factor in pK_a shift, and interactions between this residue and more distant residues can be neglected because of shielding by adjacent residues. To define the first layer, a number of parameters such as the orientation and shielding of the residues should be used. Because of limitations on the size of the data set, an excessive number of parameters could result in over-fitting. To simplify the calculation, we defined a sphere of fixed volume centered at the C α atom of the ionizable residue.

Table III

RMSD of Prediction with 20 Parameters for 405 pK_a Values

Residue	Data size	Self-consistency validation	Sixfold cross validation
Asp	134	0.557	0.728
Glu	141	0.507	0.659
His	85	0.705	1.111
Lys	45	0.425	1.845
TOTAL	405	0.562	0.982

Table IV

RMSD of Prediction with 13 Parameters For 405 pK_a Values

Residue	Data size	Self-consistency validation	Sixfold cross validation
Asp	134	0.569	0.662
Glu	141	0.521	0.609
His	85	0.769	0.990
Lys	45	0.486	1.040
TOTAL	405	0.593	0.775

Residues whose C α atom was located within the sphere were considered in the pK_a shift calculation. It was found that a sphere of radius 11 Å gave the minimum RMSD (data not show).

For each ionizable residue i (Asp, Glu, His, Lys), 20 coefficients c_{ij} were determined by fitting the data in the training set. The self-consistency and sixfold cross validation tests were performed in the prediction procedure, and the results are listed in Table III. The average RMSD between predicted and experimental values of all 405 sites for the self-consistency validation and the sixfold cross validation are 0.562 and 0.982, respectively. In common with previous prediction works,⁶⁰ the results demonstrate a gap in RMSD between the prediction performance of the self-consistency validation and the sixfold cross validation. The gap increases with decreasing size of the data set. The largest data set with 141 sites of residue Glu produced RMSD values of 0.507/0.659 for self-consistency/sixfold cross validation, while the smallest data set with 45 sites of residue Lys yielded RMSD values of 0.425/1.845.

The above results demonstrate that prediction using 20 parameters could result in over-fitting due to limitations of data set size. To avoid over-fitting, the parameters were reduced by classifying the 20 amino acids into 13 groups: His, Cys and Tyr were treated as His (with functional group —XH, X = O or N); Arg and Lys as Lys (with functional group: —NH₃); Asn and Gln as Asn (with functional group: —CONH₂); Ala, Gly, Leu, and Val as Ala (hydrophobic residues); and the rest remains ungrouped. Prediction using 13 parameters produced an obvious improvement in the sixfold cross validation as shown in Table IV. The RMSD of the sixfold cross validation for 405 pK_a values decreased from 0.982 with 20 parameters to 0.775 with 13 parameters. The improvement in prediction for residue Lys was especially apparent, where the RMSD of the sixfold cross validation prediction decreased from 1.845 with 20 parameters to 1.0 with 13 parameters. Further attempts at reducing the amino acid alphabet or reclassification produced no obvious improvements in RMSD (data not shown). The correlation plots between experimental pK_a values and predictions calculated with 13 parameters are presented in Figure 2. These plots show that most of the calculated

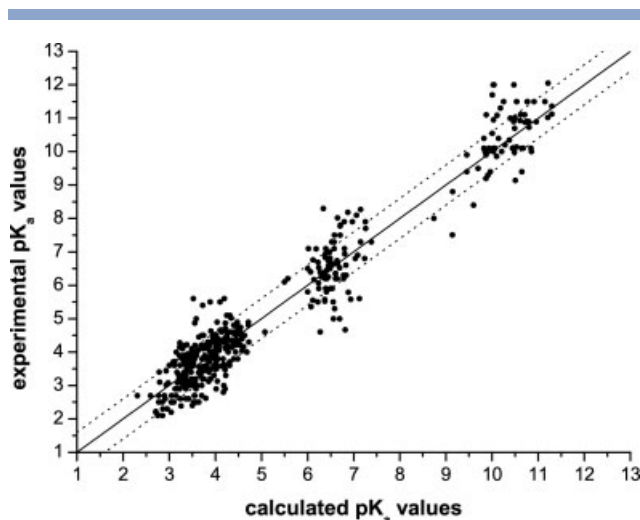


Figure 2

Correlation plots between experimental and calculated pK_a values for all 429 ionizable sites (134 Asp, 141 Glu, 85 His, 45 Lys, 3 Cys, and 21 Tyr). The solid line is the diagonal and the dotted lines represent 0.6 pH unit deviation from experimental values.

values are within 0.6 pH units of the corresponding experimental values.

In the current data set, data for Cys and Tyr was insufficient for parameter fitting and data for residue Arg was not available. To extend the prediction program to these three residues, the coefficients for His were used for the prediction of Cys and Tyr, since they share the same functional group $'-XH'$ ($X = O$ or N). The RMSD of residues Cys and Tyr is ~ 1 pH unit (Table V). We therefore suggest that the coefficients for Lys could also be used for the prediction of residue Arg, considering the common functional group $'-NH_3'$.

Approximately 10% of the ionizable residues with highly shifted pK_a values are located in an unusual environment. The real scientific challenge is to accurately predict these pK_a values. Unfortunately, the present method based on statistical approach is not suitable to predict these pK_a values due to the limitation of the data size. The average RMSD of prediction for these 46 sites is greater than 4 pH units, which indicates that these residues should be treated separately (the results are listed in Table VI and illustrated in Figure 3).

Table V

RMSD of Prediction for Cys and Tyr with the Coefficients of His

Residue	Data size	20 parameters	13 parameters
Cys	3	1.241	1.050
Tyr	21	1.080	1.067

Table VI

RMSD of Prediction for 46 pK_a Values Listed in Table II with 13 Parameters Obtained from Training Set of 405 pK_a Values

Residue	Data size	RMSD
Asp	16	3.252
Glu	5	2.112
Lys	2	7.723
His	11	3.442
Cys	5	6.666
Tyr	7	4.938
Total	46	4.258

DISCUSSION

In this study, we propose a simple model for calculation of amino acid pK_a values in proteins. Despite its simplicity, the model exhibits good prediction performance. Compared with other theoretical models and empirical prediction methods described in the literature, our model contains several significant differences.

In our model, pK_a values derived from model compounds (pK_a^{mod}) are replaced by average values derived from a database (pK_a^0). The advantage of this replacement is that some specific parameters such as dielectric constants for the protein or the solvent are omitted. Because the experimentally determined pK_a values show a normal distribution, the value of pK_a^0 differs from that of pK_a^{mod} by a constant obtained automatically from the fitting procedure.

The outcome of pK_a calculations based on macroscopic electrostatic models critically depends on the choice of protein dielectric constant, but defining this value is not straightforward. To establish the difference between vari-

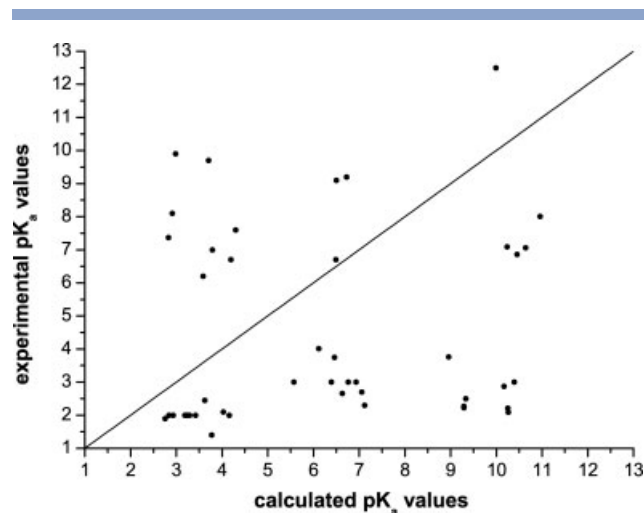


Figure 3

Correlation plots between experimental and calculated pK_a values for 46 ionizable sites which have large pK_a shift as listed in Table II (16 Asp, 5 Glu, 11 His, 2 Lys, 5 Cys, and 7 Tyr). The solid line is the diagonal.

ous macroscopic and semimacroscopic models and to illustrate the nature of the protein dielectric constants, Schutz and Warshel¹⁹ proposed a discriminative benchmark that mainly included residues whose pK_a values were shifted significantly from their values in water, and they asserted that the optimal dielectric constant for self-energies is not the optimal dielectric constant for charge–charge interactions. The protein dielectric constant is not a universal constant but simply a parameter that depends on the model used. In our study, the ΔG term in the pK_a calculation appears in a very simple form with only 20 (or 13 in a reduced alphabet) residue-type parameters. Because proteins are made of amino acid building blocks, residue–residue interactions include not only electrostatic interactions but also other types such as van der Waals interactions, which are usually ignored by models described in the literature. Furthermore, in this model, the ΔG term of the pK_a shift is proportional to the number of amino acids surrounding the residue of interest, since buried residues are surrounded by more neighbors than residues exposed to solvent. This is consistent with previous studies asserting that a relationship exists between solvent accessibility surface area (ASA) and pK_a values: pK_a values tend to decrease with increasing ASA.⁵

During NMR experiments to determine pK_a values, there are changes in the charge states of the residue of interest and surrounding residues, and the protein is constantly undergoing conformational fluctuations in response to changing solution pH. However, techniques for including conformational flexibility in titration calculations are still under development. The methods applied so far have several shortcomings; for instance, the chosen conformational ensemble does not necessarily adequately represent the protein conformational space over the investigated pH range, and no conformational variation of the protein backbone is currently allowed during the computational titration.¹⁷ The NMR experiments for determining protein pK_a values show that with a few exceptions, the pH dependency of the chemical shifts of the ionizable residues could be fitted by the Henderson-Hasselbach equation.^{6–10} This suggests that the free energy change of the proton binding reaction is unchanged during the change in pH. It is most likely that the protein structure does not sample all the conformations, rather only the ensemble whose proton binding free energy change can be compensated by conformational change. Despite the fact that the model presented here ignores both conformational changes and changes of the residue charge state, it performs quite well in predicting pK_a values.

Despite its relative simplicity, the model is quite capable of reproducing experimental results. The principal shortcoming of this statistical model is the dependence on the size of the data set. In order to reduce fitting parameters, the model neglects the orientation and shielding of residues surrounding the amino acid of interest, and this omission could introduce errors into the prediction. Furthermore, the

current data set is too small to derive prediction coefficients for Cys and Tyr as well as residues with great pK_a shift. An increase in the number of experimentally determined pK_a values would overcome this shortcoming and further enhance the accuracy of our model.

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